



Objective 4.1 To understand integral exponents

4

1. Given $2^5 = 32$,

- a) What is the base? 2
- b) What is the solution? 32
- c) What is the exponent? 5

2. Given $10^3 = 1000$,

- a) What is the power? 1000
- b) What is the exponent? 3
- c) What is the base? 10

3. Determine the value of the following powers.

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|------------------------|-----------------------|-----------------------|
| a) $6^3 =$ <u>216</u> | b) $8^2 =$ <u>64</u> | c) $3^2 =$ <u>9</u> |
| d) $4^1 =$ <u>4</u> | e) $7^2 =$ <u>49</u> | f) $5^3 =$ <u>125</u> |
| g) $10^2 =$ <u>100</u> | h) $2^3 =$ <u>8</u> | i) $2^5 =$ <u>32</u> |
| j) $4^4 =$ <u>256</u> | k) $9^3 =$ <u>729</u> | l) $0^4 =$ <u>0</u> |

4. Find the missing exponent.

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|--|--|---|
| a) $10^{\square} = 10\ 000$ $\square =$ <u>4</u> | b) $5^{\square} = 625$ $\square =$ <u>4</u> | c) $3^{\square} = 27$ $\square =$ <u>3</u> |
| d) $2^{\square} = 128$ $\square =$ <u>7</u> | e) $7^{\square} = 1$ $\square =$ <u>0</u> | f) $10^{\square} = 10$ $\square =$ <u>1</u> |
| g) $4^{\square} = 64$ $\square =$ <u>3</u> | h) $13^{\square} = 169$ $\square =$ <u>2</u> | i) $2^{\square} = 1$ $\square =$ <u>0</u> |
| j) $6^{\square} = 1296$ $\square =$ <u>4</u> | k) $20^{\square} = 400$ $\square =$ <u>2</u> | l) $8^{\square} = 512$ $\square =$ <u>3</u> |

5. Determine the base.

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|-------------------------------------|--------------------------------|---------------------------------|
| a) <u>1</u> ¹⁰ = 1 | b) <u>5</u> ³ = 125 | c) <u>14</u> ² = 196 |
| d) <u>08</u> ² = 64 | e) <u>4</u> ³ = 64 | f) <u>2</u> ⁶ = 64 |
| g) <u>10</u> ⁵ = 100 000 | h) <u>3</u> ⁴ = 81 | i) <u>24</u> ¹ = 24 |
| j) <u>2</u> ⁴ = 16 | k) <u>3</u> ⁵ = 243 | l) <u>10</u> ² = 100 |

6. Write in expanded factor form.

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|--|--|
| a) $3^4 =$ <u>$3 \times 3 \times 3 \times 3$</u> | b) $7^2 =$ <u>7×7</u> |
| c) $m^5 =$ <u>$m \times m \times m \times m \times m$</u> | d) $a^3 =$ <u>$a \cdot a \cdot a$</u> |
| e) $5^2 =$ <u>5×5</u> | f) $b^1 =$ <u>b</u> |

7. Write each of the following numbers in exponential form.

a) $49 = 7^2$ b) $125 = 5^3$ c) $216 = 6^3$
d) $32 = 2^5$ e) $27 = 3^3$ f) $169 = 13^2$

8. Express each word as power of 10.

a) A thousand. 10^3 b) A hundred thousand. 10^5 c) One. 10^0
d) One million. 10^6 e) One tenth. 10^{-1} f) One thousandth. 10^{-3}

9. Complete the property of the exponents.

1. Given a base m and an integer exponent $a > 1$,

$$m^a = \underbrace{m \cdot m \cdot m \cdots m}_{a \text{ times}}$$

2. Given a base m and the exponent 1,

$$m^1 = m$$

3. Given a base $m \neq 0$ and the exponent 0,

$$m^0 = 1$$

4. Given a base $m \neq 0$ and an integer exponent $a > 0$,

$$m^{-a} = \frac{1}{m^a}$$

5. Given a base $m > 0$ and the exponent $1/2$,

$$m^{1/2} = \sqrt{m}$$

10. Determine the power of the following expressions.

a) $3^2 = 9$ b) $5^1 = 5$ c) $8^0 = 1$
d) $6^2 = 36$ e) $9^{1/2} = 3$ f) $7^3 = 343$
g) $2^1 = 2$ h) $5^0 = 1$ i) $10^{-1} = \frac{1}{10}$
j) $16^{1/2} = 4$ k) $2^4 = 16$ l) $6^1 = 6$
m) $3^0 = 1$ n) $2^{-1} = \frac{1}{2}$ o) $100^{1/2} = 10$

11. Determine the power of the following expressions.

a) $(-3)^2 = 9$ b) $(-3)^4 = 81$ c) $(-3)^6 = 729$
d) $(-3)^1 = -3$ e) $(-3)^3 = -27$ f) $(-3)^5 = -243$

12. What can you conclude from the results obtained in 11?

Negative base with an even exponent gives a positive power.
Negative base with an odd exponent gives a negative power.